## Zero

## Explain how Europe benefited from cultural diffusion during the period c. A.D. 1000-1500.

The first evidence of zero is from the Sumerian culture in Mesopotamia, some 5,000 years ago. There, a slanted double wedge was inserted between cuneiform symbols for numbers, written positionally, to indicate the absence of a number in a place (as we would write 102, the " 0 " indicating no digit in the tens column).

The symbol changed over time as positional notation, for which zero was crucial, made its way to the Babylonian empire and from there to India, via the Greeks (in whose own culture zero made a late and only occasional appearance; the Romans had no trace of it at all).

Arab merchants brought the zero they found in India to the West, and after many adventures and much opposition, the symbol we use took hold and the concept flourished, as zero took on much more than a positional meaning and has played a crucial role in our mathematizing of the world.

The path that leads to the discovery of " 0 " lies only in the most advanced type of number system, which is called "positional" because the value of a character depends on its position. Our modern way of counting is positional. The base figure " 5 " has a different value in 514 and in 145, determined by its position.

You come across a big stumbling block when you try to write a number like 2,002. For a Roman, who used an additive numbering system, that is not a problem: MMII. But in a positional system, a way must be found to indicate the absence of "tens" and "hundreds." A gap could be left(the Babylonians did this at first), but that opens the door to more scribal errors, and anyway how does one indicate two gaps, as in 2,002?

It becomes necessary to have a "zero," a character that signifies "empty." Maybe not necessary, because the brilliant Chinese mathematicians somehow managed to run a positional system without making this discovery. The Babylonians (eventually), the Indians, and the Mayans did discover it, however.

But the next step, the true miracle moment, is to realize that the "symbol for nothing" that is being used is not just a place-
 holder, but an actual number: that "empty" and "nothing" are one. The null number is as real as " 5 " and " 2,002 ". Without this, there is no modern mathematics, no algebra, no modern science.

